

1. [2 marks] A feasible set has vertices $(0,3)$, $(5,0)$ and $(2,5)$. Find the maximum value of $5x + 2y$ on the feasible set and state the point where the maximum occurs.

Vertices	$5x + 2y$
$(0,3)$	6
$(5,0)$	25
$(2,5)$	20

The maximum value is 25 and it occurs at the point $(5,0)$.

2. [3 marks] Find the equation of the line that is perpendicular to $y = \frac{2}{3}x + 7$ and that passes through the point $(6, -11)$.

$y = \frac{2}{3}x + 7$ has $m = \frac{2}{3}$
Desired line has $m = -\frac{3}{2}$
(the lines are perpendicular).

Desired line: $y = mx + b$

$$y = -\frac{3}{2}x + b$$

Sub $x=6$, $y=-11$: $-11 = -\frac{3}{2}(6) + b$

$$-11 = -9 + b$$

$$-2 = b$$

$$y = -\frac{3}{2}x - 2$$

3. [3 marks] List all the inequalities that apply:

A company makes backpacks and purses. Each backpack takes 4 hours to sew and 2 hours to dye. Each purse takes 5 hours to sew and 1 hour to dye. Each day the company has at most 100 sewing hours and at most 40 dyeing hours available. Let x be the number of backpacks made each day and let y be the number of purses made each day.

	^(x) Backpacks	^(y) Purses	Available
Sew (hours)	4	5	100
Dye (hours)	2	1	40

\swarrow number of objects
 \swarrow can't be negative

$$4x + 5y \leq 100, 2x + y \leq 40, x \geq 0, y \geq 0$$

4. [3 marks] Find the intersection of $8x + 2y = -12$ and $-2x + y = 12$.

$$8x + 2y = -12$$

$$2y = -12 - 8x$$

$$y = -6 - 4x$$

$$-2x + y = 12$$

$$y = 12 + 2x$$

$$y = y$$

$$-6 - 4x = 12 + 2x$$

$$-6x = 18$$

$$x = -3$$

$$x = -3 \rightarrow \text{either equation}$$

$$y = 12 + 2x$$

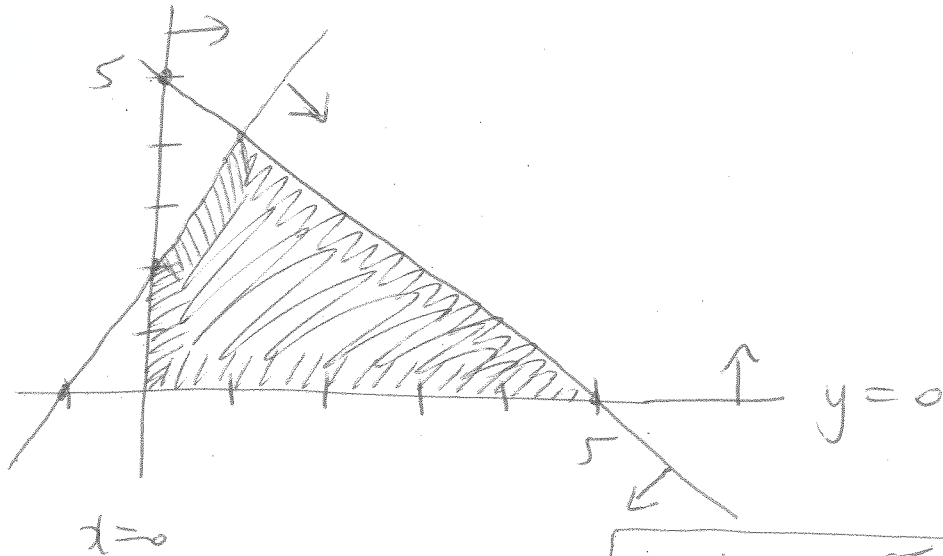
$$y = 12 - 6$$

$$y = 6$$

$$(-3, 6)$$

5. [2 marks] Graph the feasible set for the following system of inequalities:

$$x + y \leq 5, \quad -2x + y \leq 2, \quad x \geq 0, \quad y \geq 0$$



$$\begin{aligned}
 &-2x + y = 2 \\
 &(-1, 0) \\
 &(0, 2) \\
 &\text{Test } (0, 0): \text{TRUE}
 \end{aligned}$$

$$\begin{aligned}
 &x + y = 5 \\
 &(5, 0) \\
 &(0, 5) \\
 &\text{Test } (0, 0): \text{TRUE}
 \end{aligned}$$

6. [3 marks] Solve the following system using Gauss-Jordan Elimination:

$$x - 4y = -23$$

$$2x - 7y = -38$$

$$\begin{array}{cc|c} x & y & \# \\ \hline 1 & -4 & -23 \\ 2 & -7 & -38 \end{array}$$

$$R_2 - 2R_1 \quad \begin{array}{cc|c} 1 & -4 & -23 \\ \hline 0 & 1 & 8 \end{array}$$

$$R_1 + 4R_2 \quad \begin{array}{cc|c} 1 & 0 & 9 \\ \hline 0 & 1 & 8 \end{array}$$

$$x = 9$$

$$y = 8$$

7. [4 marks] Solve the following system using Gauss-Jordan Elimination:

$$x + y + z = 6$$

$$2x + 4y = 14$$

$$5x + 9y + z = 34$$

$$\begin{array}{ccc|c} x & y & z & \# \\ \hline 1 & 1 & 1 & 6 \\ 2 & 4 & 0 & 14 \\ 5 & 9 & 1 & 34 \end{array}$$

$$\begin{array}{l} R_2 - 2R_1 \\ R_3 - 5R_1 \end{array} \quad \begin{array}{ccc|c} 1 & 1 & 1 & 6 \\ 0 & 2 & -2 & 2 \\ 0 & 4 & -4 & 4 \end{array}$$

$$\frac{R_2}{2} \quad \begin{array}{ccc|c} 1 & 1 & 1 & 6 \\ 0 & 1 & -1 & 1 \\ 0 & 4 & -4 & 4 \end{array}$$

$$\begin{array}{l} R_1 - R_2 \\ R_3 - 4R_2 \end{array} \quad \begin{array}{ccc|c} \textcircled{1} & 0 & 2 & 5 \\ 0 & \textcircled{1} & -1 & 1 \\ 0 & 0 & 0 & 0 \end{array}$$

$z = \text{any value}$

$$x + 2z = 5 \Rightarrow x = 5 - 2z$$

$$y - z = 1 \Rightarrow y = 1 + z$$