

Name: \_\_\_\_\_

**Marks may be deducted for not showing all your work.**

1. [3 marks] The lifetime of a machine part is exponentially distributed with probability density function  $f(x) = 0.2e^{-0.2x}$ , where  $x$  is measured in years. Find the probability that the part lasts at most 8 years. Round your answer to three decimal places.

2. [3 marks] A website receives an average of 120 visits per day. Find the probability that the website receives at least three visits in the next hour. Round your answer to three decimal places.

3. [3 marks] At an engineering firm, employees worked a mean of 57 hours last week, with a standard deviation of 4 hours. Find the probability that a group of 40 randomly selected employees worked a total of more than 2300 hours last week.

4. [4 marks] A coin lands on heads 52% of the time. Estimate the probability of observing between 180 and 195 heads (inclusive) in 400 tosses of the coin.

5. [4 marks] We want to estimate a population proportion with a 98% margin of error at most 0.05. We have no information about  $\hat{p}$ . What is the minimum sample size we can use when collecting the sample data?

6. [2 marks] We are testing the hypothesis  $H_0: \mu = 220$  with  $\alpha = 0.05$ . We are given  $\bar{x} = 212$ ,  $s = 16$  and  $n = 64$ .

a) Define a Type I error.

b) Find the probability of a Type I error.

7. [6 marks] Test whether the two population means are equal at the 2% significance level given the following sample data:

$$n_1 = 100, \bar{x}_1 = 81.4, s_1 = 3.1, n_2 = 60, \bar{x}_2 = 82.2, s_2 = 1.9.$$

a) State  $H_0$  and  $H_a$

b) Check any necessary assumptions.

c) Do you reject  $H_0$ ? Show all your work.

d) Find the  $p$ -value.