

Solutions 3.

$$\textcircled{1} \quad \text{mean} = \frac{27+45+\dots+38}{10} = 37.8$$

Ordered: 27, 32, 33, 34, 36, 38, 39, 45, 45, 49

$$\text{Median} = \frac{36+38}{2} = 37$$

Mode: 45

$\textcircled{2}$ Median < Mean
skewed to the right

$$\textcircled{3} \quad \text{mean} = \frac{36.8(4) + 37.1(6) + \dots + 37.7(8)}{25} = 37.312^\circ\text{C}$$

mode = 37.7°C (most frequently occurring)

Median is the $0.5(25+1) = 13^{\text{th}}$ measurement
when data is ordered.

$$\text{Median} = 37.4^\circ\text{C}$$

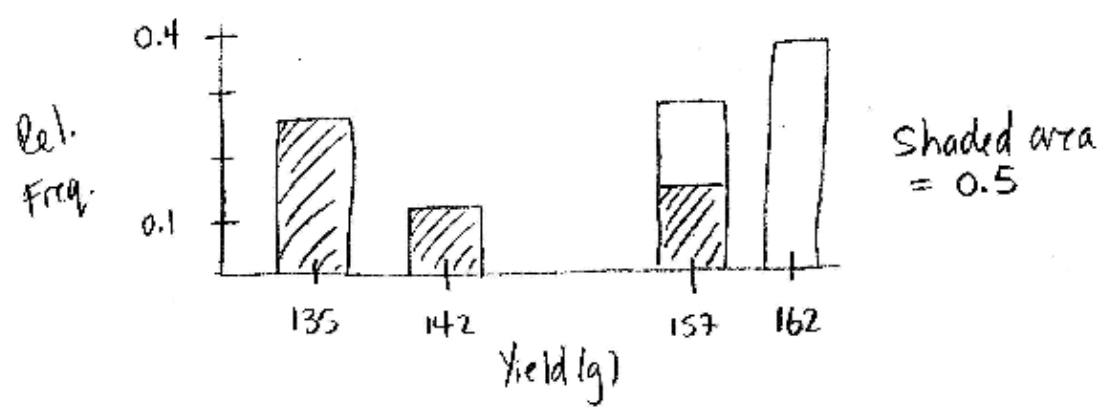
$\textcircled{4}$ Caution: Data is not ordered
In order:

Yield (g)	Relative Frequency
135	0.24
142	0.13
157	0.25
162	0.38

mean = $135(0.24) + \dots + 162(0.38) = 151.67 \text{ g}$

mode = 162 g (most frequently occurring)

median: histogram might be helpful



median = 157 g

⑤

30	1 8 7
31	7 8 1
32	1 2 5 5 6
33	4 3 4 4 9

→

30	1 7 8
31	1 7 8
32	1 2 5 5 6
33	3 4 4 4 9

a) mean = 322.1875

b) median = $\frac{322 + 325}{2} = 323.5$

c) mode = 334

d) 4th smallest measurement = 311

⑥ Position is $0.5(1013+1) = 507$
The 507^{th} measurement is the median.

⑦ Position is $0.5(500+1) = 250.5$
The median is the average of the
 250^{th} and the 251^{st} measurements.

⑧ Let $x = 4^{\text{th}}$ test mark
Want $\frac{65+72+78+x}{4} = 75$

$$65+72+78+x = 300$$

$$x = 85$$

The student must earn 85 on the 4^{th} test.

⑨ Let x_1, x_2, x_3, x_4 be the 4 test marks.

Given $\frac{x_1+x_2+x_3}{3} = 67$ ①

Want $\frac{x_1+x_2+x_3+x_4}{4} = 73$ ②

①: $x_1+x_2+x_3 = 201$ ③

②: $x_1+x_2+x_3+x_4 = 292$ ④

④ - ③: $x_4 = 91$

The 4^{th} test mark must be 91.

10 Estimate using the mean of the endpoints:

	Score	Frequency
$\frac{50+60}{2}$ →	55	3
	65	11
$\frac{60+70}{2}$ →	75	22
	85	6
	95	4
$\frac{90+100}{2}$ →		

$$\text{mean} \approx \frac{55(3) + 65(11) + \dots + 95(4)}{46}$$

$$\approx 74.3$$