

Name: _____

Find the linearization of $f(x) = x^{\frac{1}{3}}$ at $x = 125$.

Given: $f(x) \approx f(a) + f'(a)(x - a)$

$$a = 125$$

$$f(125) = 125^{\frac{1}{3}} = 5$$

$$f'(x) = \frac{1}{3} x^{-\frac{2}{3}}$$

$$\begin{aligned} f'(125) &= \frac{1}{3} \cdot \sqrt[3]{\frac{1}{125^2}} \\ &= \frac{1}{3} \cdot \frac{1}{25} \\ &= \frac{1}{75} \end{aligned}$$

$$f(x) \approx f(125) + f'(125)(x - 125)$$

$$x^{\frac{1}{3}} \approx 5 + \frac{1}{75}(x - 125)$$

Valid near $x = 125$