

Name: _____

Given $y = (1 + 2x)^3$ and $\frac{dx}{dt} = 1.5$ units/s, find $\frac{dy}{dt}$ when $y = 27$.

1) Equation
$$y = (1 + 2x)^3$$

2) Take $\frac{d}{dt}$

$$\begin{aligned}\frac{dy}{dt} &= \frac{dy}{dx} \frac{dx}{dt} \\ &= 3(1 + 2x)^2 (2) \frac{dx}{dt}\end{aligned}$$

3) Missing Values

$$y = 27 \rightarrow y = (1 + 2x)^3$$

$$27 = (1 + 2x)^3$$

$$3 = 1 + 2x$$

$$x = 1$$

4) Solve

$$\begin{aligned}\frac{dy}{dt} &= 3(1 + 2x)^2 (2) \frac{dx}{dt} \\ &= 3(3)^2 (2) (1.5) \\ &= 81 \frac{\text{units}}{\text{s}}\end{aligned}$$