

1. [4 marks] Given that  $p$  is TRUE and  $q$  is FALSE, state whether each proposition is TRUE or FALSE:

a)  $p \oplus q$

TRUE

b)  $\sim q \vee p$

TRUE

c)  $\sim (q \vee p)$

FALSE

d)  $\sim q \wedge p$

TRUE

2. [4 marks] a) Build the truth table for  $(\sim p \wedge q) \vee (p \wedge \sim q)$ .

$p$	$q$	$\sim p$	$\sim p \wedge q$	$\sim q$	$p \wedge \sim q$	$(\sim p \wedge q) \vee (p \wedge \sim q)$
0	0	1	0	1	0	0
0	1	1	1	0	0	1
1	0	0	0	1	1	1
1	1	0	0	0	0	0

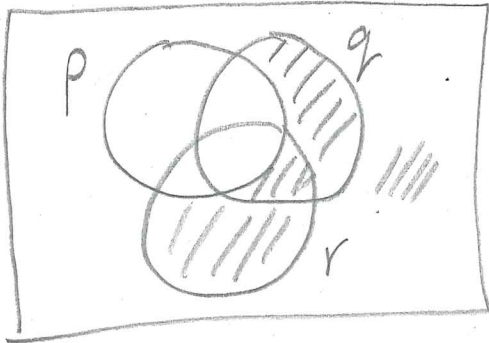
Question 2 was removed from the test.

b) Is  $(\sim p \wedge q) \vee (p \wedge \sim q)$  logically equivalent to  $p \oplus q$ ? State YES or NO.

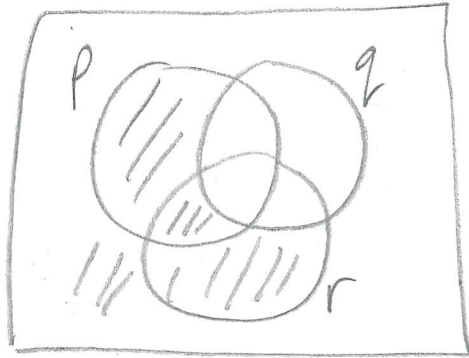
$p$	$q$	$p \oplus q$
0	0	0
0	1	1
1	0	1
1	1	0

YES (Columns are identical.)

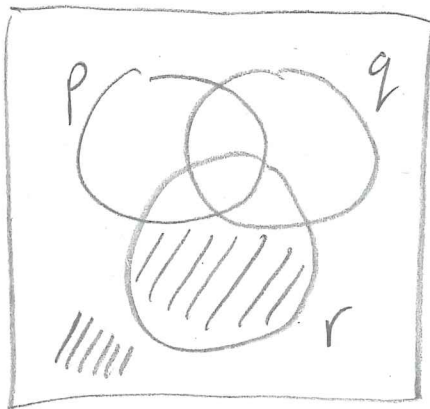
3. [4 marks] Draw the Venn diagram for  $(\sim p \wedge \sim q) \vee r$ .



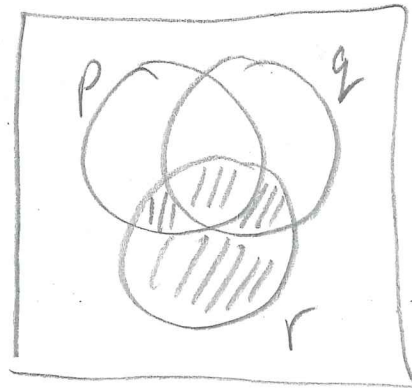
$\sim p$



$\sim q$



$\sim p \wedge \sim q$



$(\sim p \wedge \sim q) \vee r$

4. [6 marks] Convert to decimal:

a)  $DAE5_{16}$

$$\begin{aligned} &= D \times 16^3 + A \times 16^2 + E \times 16^1 + 5 \times 16^0 \\ &= 13 \times 16^3 + 10 \times 16^2 + 14 \times 16 + 5 \\ &= 56\,037 \end{aligned}$$

b)  $372.64_8$

$$\begin{aligned} &= 3 \times 8^2 + 7 \times 8^1 + 2 \times 8^0 + 6 \times 8^{-1} + 4 \times 8^{-2} \\ &= 3 \times 8^2 + 7 \times 8 + 2 + \frac{6}{8} + \frac{4}{8^2} \\ &= 250.8125 \end{aligned}$$

5. [4 marks] Convert 85.71875 to octal.

$85 \div 8$	Q	R
	10	5
$10 \div 8$	1	2
$1 \div 8$	0	1

$0.71875 \times 8$	I	N
	5	0.75
$0.75 \times 8$	6	0

125.56<sub>8</sub>

6. [3 marks] Convert 0.3 to binary.

$0.3 \times 2$	I	N
	0	0.6
$0.6 \times 2$	1	0.2
$0.2 \times 2$	0	0.4
$0.4 \times 2$	0	0.8
$0.8 \times 2$	1	0.6
$0.6 \times 2$		

0.01001<sub>2</sub>